

**Aarhus Convention Compliance Committee
Communication ACCC/C/2013/82:
Johnstone v. Norway¹**

Annexure “E”

**Only Civilization Collapse will prevent
runaway global climate change:
Industrial Civilization/Consumption
Developmentism as ‘Heat Engine’ Root
cause of Scarcity-Conflict Climate
Change-National Security Impending
Near-term Extinction reality.**

University of Utah (22 Nov 2009): *Is Global Warming Unstoppable?: Theory also says Energy Conservation doesn't help*².

Timothy J. Garrett (Nov. 2009), *Are there basic physical constraints on future anthropogenic emissions of carbon dioxide?*³; Climatic Change

¹ <http://ecofeminist-v-breivik.weebly.com/unece-aarhus-comp-comm.html>

² http://unews.utah.edu/news_releases/is-global-warming-unstoppable/

³ <http://link.springer.com/article/10.1007%2Fs10584-009-9717-9>

Campus Life from the U

Is Global Warming Unstoppable?

THEORY ALSO SAYS ENERGY CONSERVATION DOESN'T HELP



Nov. 22, 2009 – In a provocative new study, a University of Utah scientist argues that rising carbon dioxide emissions – the major cause of global warming – cannot be stabilized unless the world's economy collapses or society builds the equivalent of one new nuclear power plant each day.

"It looks unlikely that there will be any substantial near-term departure from recently observed acceleration in carbon dioxide emission rates," says the new paper by Tim Garrett, an associate professor of atmospheric sciences.

Garrett's study was panned by some economists and rejected by several journals before acceptance by *Climatic Change*, a journal edited by renowned Stanford University climate scientist Stephen Schneider. The study will be published online this week.

The study – which is based on the concept that physics can be used to characterize the evolution of civilization – indicates:

- Energy conservation or efficiency doesn't really save energy, but instead spurs economic growth and accelerated energy consumption.
- Throughout history, a simple physical "constant" – an unchanging mathematical value – links global energy use to the world's accumulated economic productivity, adjusted for inflation. So it isn't necessary to consider population growth and standard of living in predicting society's future energy consumption and resulting carbon dioxide emissions.
- "Stabilization of carbon dioxide emissions at current rates will require approximately 300 gigawatts of new non-carbon-dioxide-emitting power production capacity annually – approximately one new nuclear power plant (or equivalent) per day," Garrett says. "Physically, there are no other options without killing the economy."

Getting Heat for Viewing Civilization as a "Heat Engine"

Garrett says colleagues generally support his theory, while some economists are critical. One economist, who reviewed the study, wrote: "I am afraid the author will need to study harder before he can contribute."

"I'm not an economist, and I am approaching the economy as a physics problem," Garrett says. "I end up with a global economic growth model different than they have."

Garrett treats civilization like a "heat engine" that "consumes energy and does 'work' in the form of economic production, which then spurs it to consume more energy," he says.

"If society consumed no energy, civilization would be worthless," he adds. "It is only by consuming energy that civilization is able to maintain the activities that give it economic value. This means that if we ever start to run out of energy, then the value of civilization is going to fall and even collapse absent discovery of new energy sources."

Garrett says his study's key finding "is that accumulated economic production over the course of history has been tied to the rate of energy consumption at a global level through a constant factor."

That "constant" is 9.7 (plus or minus 0.3) milliwatts per inflation-adjusted 1990 dollar. So if you look at economic and energy production at any specific time in history, "each inflation-adjusted 1990 dollar would be supported by 9.7 milliwatts of primary energy consumption," Garrett says.

Garrett tested his theory and found this constant relationship between energy use and economic production at any given time by using United Nations statistics for global GDP (gross domestic product), U.S. Department of Energy data on global energy consumption during 1970-2005, and previous studies that estimated global economic production as long as

Join the Conversation



Search the Archives

Year Month

Category

2,000 years ago. Then he investigated the implications for carbon dioxide emissions.

"Economists think you need population and standard of living to estimate productivity," he says. "In my model, all you need to know is how fast energy consumption is rising. The reason why is because there is this link between the economy and rates of energy consumption, and it's just a constant factor."

Garrett adds: "By finding this constant factor, the problem of [forecasting] global economic growth is dramatically simpler. There is no need to consider population growth and changes in standard of living because they are marching to the tune of the availability of energy supplies."

To Garrett, that means the acceleration of carbon dioxide emissions is unlikely to change soon because our energy use today is tied to society's past economic productivity.

"Viewed from this perspective, civilization evolves in a spontaneous feedback loop maintained only by energy consumption and incorporation of environmental matter," Garrett says. It is like a child that "grows by consuming food, and when the child grows, it is able to consume more food, which enables it to grow more."

Is Meaningful Energy Conservation Impossible?

Perhaps the most provocative implication of Garrett's theory is that conserving energy doesn't reduce energy use, but spurs economic growth and more energy use.

"Making civilization more energy efficient simply allows it to grow faster and consume more energy," says Garrett.

He says the idea that resource conservation accelerates resource consumption – known as Jevons paradox – was proposed in the 1865 book "The Coal Question" by William Stanley Jevons, who noted that coal prices fell and coal consumption soared after improvements in steam engine efficiency.

So is Garrett arguing that conserving energy doesn't matter?

"I'm just saying it's not really possible to conserve energy in a meaningful way because the current rate of energy consumption is determined by the unchangeable past of economic production. If it feels good to conserve energy, that is fine, but there shouldn't be any pretense that it will make a difference."

Yet, Garrett says his findings contradict his own previously held beliefs about conservation, and he continues to ride a bike or bus to work, line dry family clothing and use a push lawnmower.

An Inevitable Future for Carbon Dioxide Emissions?

Garrett says often-discussed strategies for slowing carbon dioxide emissions and global warming include mention increased energy efficiency, reduced population growth and a switch to power sources that don't emit carbon dioxide, including nuclear, wind and solar energy and underground storage of carbon dioxide from fossil fuel burning. Another strategy is rarely mentioned: a decreased standard of living, which would occur if energy supplies ran short and the economy collapsed, he adds.

"Fundamentally, I believe the system is deterministic," says Garrett. "Changes in population and standard of living are only a function of the current energy efficiency. That leaves only switching to a non-carbon-dioxide-emitting power source as an available option."

"The problem is that, in order to stabilize emissions, not even reduce them, we have to switch to non-carbonized energy sources at a rate about 2.1 percent per year. That comes out to almost one new nuclear power plant per day."

"If society invests sufficient resources into alternative and new, non-carbon energy supplies, then perhaps it can continue growing without increasing global warming," Garrett says.

Does Garrett fear global warming deniers will use his work to justify inaction?

"No," he says. "Ultimately, it's not clear that policy decisions have the capacity to change the future course of civilization."

Media Contacts For This Story

Tim Garrett
associate professor of atmospheric sciences

Office Phone: (801) 581-5768
Email address: tim.garrett@utah.edu

Lee J. Siegel
science news specialist, University of Utah
Communications

Office Phone: 801-581-8993
Cell Phone: 801-244-5399
Email address: lee.siegel@utah.edu

[◀ Previous Story](#)**U News Archives**[Next Story ▶](#)**Social Media**

-  News from the U on Twitter
-  The University of Utah on Twitter
-  Events at the U on Twitter
-  RedThread: The Us blog
-  The University of Utah on Facebook
-  The University of Utah on YouTube
-  The University of Utah on Vimeo

Campus Information

- Community Forum
- FYI Faculty/Staff Newsletter
- KUED
- KUER
- K-UTE
- The Daily Utah Chronicle
-  U of U Facts
- Veterans Day Commemoration
- University Marketing & Communications

 **EVENTS**

- May 13 | Summer Institute on Teaching Linguistically and Culturally Diverse Students
- May 13 | Critical Infrastructure Town Hall Meeting
- May 14 | Summer Institute on Teaching Linguistically and Culturally Diverse Students
- May 14 | Non-Credit Letterpress

[VISIT EVENTS WEBSITE ▶](#)

UNIVERSITY OF UTAH PUBLIC RELATIONS | 201 PRESIDENTS CIRCLE ROOM 308, SALT LAKE CITY, UTAH 84112 | 801-585-9244 | FAX 801-585-3350

©2013 THE UNIVERSITY OF UTAH | [CONTACT](#) | [DISCLAIMER](#) | [PRIVACY](#)

Are there basic physical constraints on future anthropogenic emissions of carbon dioxide?

Timothy J. Garrett

Received: 12 November 2008 / Accepted: 27 August 2009 / Published online: 21 November 2009
© The Author(s) 2009. This article is published with open access at Springerlink.com

Abstract Global Circulation Models (GCMs) provide projections for future climate warming using a wide variety of highly sophisticated anthropogenic CO₂ emissions scenarios as input, each based on the evolution of four emissions “drivers”: population p , standard of living g , energy productivity (or efficiency) f and energy carbonization c (IPCC WG III 2007). The range of scenarios considered is extremely broad, however, and this is a primary source of forecast uncertainty (Stott and Kettleborough, Nature 416:723–725, 2002). Here, it is shown both theoretically and observationally how the evolution of the human system can be considered from a surprisingly simple thermodynamic perspective in which it is unnecessary to explicitly model two of the emissions drivers: population and standard of living. Specifically, the human system grows through a self-perpetuating feedback loop in which the consumption rate of primary energy resources stays tied to the historical accumulation of global economic production—or $p \times g$ —through a time-independent factor of 9.7 ± 0.3 mW per inflation-adjusted 1990 US dollar. This important constraint, and the fact that f and c have historically varied rather slowly, points towards substantially narrowed visions of future emissions scenarios for implementation in GCMs.

1 Introduction

GCM projections of 21st century climate change use prognostic trajectories for carbon dioxide (CO₂) emission fluxes developed by the International Panel on Climate Change (IPCC) Special Report on Emissions Scenarios (SRES) (IPCC WG

T. J. Garrett (✉)
Department of Atmospheric Sciences, University of Utah,
Salt Lake City, UT, USA
e-mail: tim.garrett@utah.edu

III 2007). These provide a range of timelines, each designed to show how a given set of decisions might correspond to a particular atmospheric CO₂ trajectory. SRES models are highly sophisticated, and contain numerous interactive components, each designed to reflect a realistic range of societal dynamic behavior.

For tractability, IPCC SRES models express the primary drivers of growth in CO₂ emissions E in terms of human population p , rates of primary energy consumption a and real (or inflation-adjusted) economic production P through $E = p \times g \times i \times c$ where $g = P/p$ represents the real economic production per person and $i = 1/f = a/P$ represents the “energy intensity” of real economic production, or alternatively, the inverse of its “energy productivity” f , and $c = E/a$ the carbonization of the energy supply (Nakicenovic 2004). Expressed in a prognostic form, emissions grow at a rate given by (Nakicenovic 2004; Raupach et al. 2007)

$$\frac{d \ln E}{dt} = \frac{d \ln p}{dt} + \frac{d \ln g}{dt} - \frac{d \ln f}{dt} + \frac{d \ln c}{dt} \quad (1)$$

Differences among SRES emissions trajectories depend on how society is assumed to manage such issues as population control, energy efficiency, and a switch to non-CO₂ emitting energy resources. Currently, the range of possible futures considered is extremely broad. In fact, uncertainty in the degree of surface warming over the next century is determined as much by the range of SRES scenarios as by climate physics itself (Stott and Kettleborough 2002).

In this paper I propose that by using a straight-forward thermodynamic approach it may be possible to substantially constrain plausible timelines for future anthropogenic CO₂ emission rates.

2 A thermodynamic growth model

2.1 A heat engine

The starting point is recognition that general thermodynamic laws require that all systems, even those that are living, evolve through a spontaneous conversion of environmental potential energy into some less available form, often termed “heat” (Schrödinger 1944; de Groot and Mazur 1984; Vermeij 1995; Kleidon 2004).

Specifically, consider a system drawn in Fig. 1 consisting of some entity and its environment, separated by some arbitrarily defined permeable interface at a fixed temperature T_s and pressure p (i.e., at constant energy density or an isentrope). As a whole, the system is in contact (through radiation, convection or conduction) with colder, lower energy density surroundings at temperature $T < T_s$. The interface between the entity and the environment represents a “step”, with its height represented by a Gibbs energy potential ΔG . Available potential energy in the environment is converted at rate $a = \alpha \Delta G$ into some unavailable form through the transfer of matter across the interface. The system-specific constant coefficient α is an intensive quantity that defines the particular physics of “availability” for the system.¹

¹To take an electrostatic analogue, ΔG is a voltage difference, a a current, and $1/\alpha$ is the resistance, in which case the relevant physics defining “availability” of energy is the material’s conductivity.

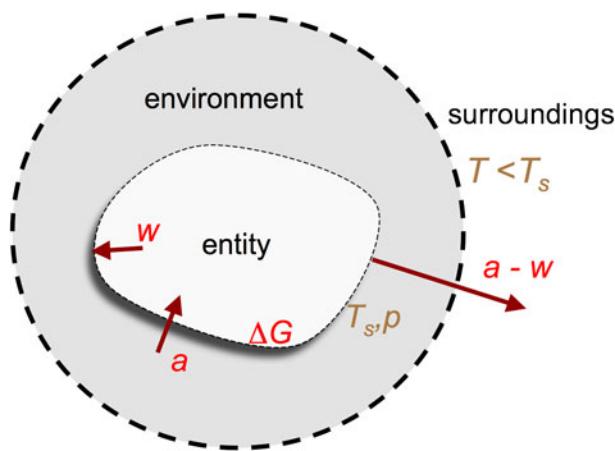


Fig. 1 Illustration of an evolving system bounding some entity and its environment, as separated by a permeable interface at constant temperature and pressure. The interface maintains an energy potential $\Delta G(T_s, p)$ so that the system as a whole is able to convert available energy at rate a into work w with efficiency $\varepsilon = w/a$, and “heat” at rate $a - w$. Heat is voided to the system’s colder surroundings; work grows the interface at rate $w = d(\Delta G)/dt$. Because the interface potential is related to energy consumption through $a = \alpha\Delta G$, where α is an engine specific constant coefficient, what is defined is a positive feedback loop in which, through work, a and ΔG evolve logarithmically at rate $d\ln a/dt = d\ln(\Delta G)/dt = \eta = \varepsilon\alpha$. Here η can be considered a feedback efficiency or rate of return

Effectively, the system operates as a form of “heat engine”. The familiar textbook heat engine has the engine consume energy at rate a to do “work” at rate w to contribute to the potential of some outside agency while releasing waste “heat” at rate $a - w$ (Zemansky and Dittman 1997). While the definition of work is clear for an industrial steam engine raising the gravitational potential of a steel beam, for example, the choice of what qualifies as work is quite subjective. In fact, all energy transfers a act to increase the potential of something. Work is simply the raised potential of interest. Heat is the remainder.

With reference to Fig. 1, work is subjectively defined with respect to the internal energy potential ΔG of the interface separating the environment and the entity. Thus, through consumption of available energy at rate a , the value of ΔG evolves at rate $w = d\Delta G/dt$ with heat engine efficiency $\varepsilon = w/a$. Meanwhile, heat is lost spontaneously to the colder surroundings at rate $a - w$. The Second Law of Thermodynamics requires that heat production $a - w > 0$, in which case ε must be less than unity. Thus, the existence of a potential difference ΔG between the entity and its environment entails decay of the available potential of the universe as a whole (or equivalently, an increase in its entropy) (Zemansky and Dittman 1997).

The advantage of the above thermodynamic setup is that it allows for spontaneous evolution of the entity, and, as will be shown, it can be applied more specifically to the evolution of civilization. Because work is internal, a feedback loop causes the interface to exponentially grow or decay: the existence of ΔG requires energy consumption at rate $a = \alpha\Delta G$; in turn, this corresponds to work being done at rate $w = \varepsilon a$, which then adds to the internal potential at rate $d\Delta G/dt = w$, closing the loop. If work increases the magnitude of ΔG , then the interface separating the entity

and its environment bootstraps itself to a higher level. Then the system as a whole evolves to higher levels of energy consumption a through

$$\frac{da}{dt} = \alpha \frac{d(\Delta G)}{dt} = \alpha w = \alpha \varepsilon a \equiv \eta a \quad (2)$$

where η is effectively a “rate of return” representing the efficiency of the feedback on energy consumption a . Note that, perhaps counter-intuitively, higher energy efficiency ε corresponds to higher values of η , and therefore more rapidly exponential evolution of energy consumption a and heat production $a - w$.

In Appendix A, the nature of the feedback efficiency η is defined more precisely. It is shown that the interface ΔG can be separated into \check{n} material units, each associated with the same potential energy at fixed temperature and pressure of $\Delta\mu$. ΔG results in a flow of material across the interface at rate $dn/dt = a/\Delta\mu$. If the net flow is *from* the environment *to* the entity, a portion of material that diffuses across the interface at rate dn/dt then contributes to interface growth at rate $d\check{n}/dt$. The feedback efficiency η is the logarithmic form for this material rate of growth

$$\eta = \frac{d \ln \check{n}}{dt} \quad (3)$$

A concrete example that might be particularly easy to relate to is the growth of a young child. As an entity, the child consumes the accessible energy contained in food from the environment in proportion to some measure of the child’s size. This rate of consumption $a = \alpha \Delta G$ —perhaps about 50 W—enables the child to do “work” at rate $w = d\Delta G/dt$ with energy efficiency $\varepsilon = w/a$, incorporating the water and nutrients contained in food into its structure in order to extend the material interface \check{n} separating it from its environment. The child maintains homeostasis because “heat” can eventually radiate to space at rate $a - w$ at a relatively cold planetary blackbody temperature of about 255 K. Material waste is also produced once the useful chemical potential of the nutrition has been extracted, for example as carbohydrates are converted to exhaled CO₂. Through a feedback loop, if $w > 0$, the child and its energy consumption grow logarithmically at a rate $\eta = d \ln a / dt$. Of course, in an energy poor environment there might not be sufficient nutrition, in which case $w < 0$ and the feedback efficiency η is negative. But, assuming the child reaches adulthood, growth tends towards a balance between energy consumption and heat production, and η tends to zero.

3 Analog for the economic growth of civilization and its CO₂ emissions

The argument now is that the thermodynamic growth model described above, just as it can be applied to a child’s growth, can also be extended to the human system in its entirety, as defined by civilization and its known environmental reservoirs. As with the child, an interface potential ΔG between civilization and its primary energy resources enables energy to be consumed at rate a . This allows work to be done with efficiency ε and at rate w to grow the interface potential ΔG through incorporation of environmental matter (e.g., biomass and minerals). Simultaneously, through convection and radiation, heat is lost to space at rate $a - w$ at the

planetary blackbody temperature. Also, unused material waste accumulates in the environment.

Of course, for civilization, “food” includes the chemical and nuclear bonds in oil, coal and uranium, combined with mineral matter from the Earth’s crust. These build structures that include not just human bones, flesh, blood and nerves, but cities, roads, shipping and telecommunications. However, insofar as the thermodynamics is concerned, the difference between the child and civilization is really only a matter of complexity and scale. In either case, as part of a single energy-consuming organism, all organism elements contribute to an interface with environmental reservoirs that enables net available energy transfer to the organism at rate a .

While a precise definition of civilization is arbitrary, civilization is most commonly quantified in purely fiscal terms. Thus, the goal here is to examine whether it is possible to link fiscal quantities to the more thermodynamic model defined above. To this end, an argument can be made that, if what physically distinguishes civilization from its environment is some thermodynamic potential ΔG at constant temperature and pressure, civilization implicitly assigns inflation-adjusted (or real) monetary value to what ΔG enables—the total rate of energy consumption a . To borrow a phrase, “money is power” because, if all current exothermic processes supporting civilization were to suddenly cease such that a equalled zero, all civilization would become worthless; it would no longer be associated with a non-equilibrium level of potential energy $\Delta G = a/\alpha$. Simply, there would be no definable material interface \dot{n} between civilization and its environment.

As an example, the potential energy in oil combustion is valuable, but only to the extent it that it can interact with the interface separating civilization from its environment. It has zero value if it burns wastefully in the desert, and zero value in its unavailable chemical and nuclear bonds. From society’s perspective, any societal element, whether living or synthetic, only has value to the extent it is able to operate in synergy with all other elements to define an interface with environmental available energy. An unavailable road from nowhere to nowhere is just pavement on the ground. But the same road between two cities is part of a larger organism that works collectively at net rate w to grow access to the primary energy supplies that civilization requires.

The mathematical expression of the above argument is that global primary energy consumption a is related to global value C through a constant factor λ

$$a = \lambda C \quad (4)$$

Thus, the economic representation of the evolving heat engine given by Eq. 2 is

$$\frac{dC}{dt} = \frac{1}{\lambda} \frac{da}{dt} = \frac{\alpha}{\lambda} \frac{d(\Delta G)}{dt} = \frac{\alpha}{\lambda} w = \frac{\eta}{\lambda} a \quad (5)$$

or in purely economic terms

$$P \equiv \frac{dC}{dt} = \eta C \quad (6)$$

where, C (units real economic value) grows through the real (inflation-adjusted) economic production rate P (units real economic value per year). The thermodynamic feedback efficiency η is an economic rate of return on C .

Equation 5 implies that real economic production P is, perhaps rather intuitively, only a measure of thermodynamic work w through coefficient α/λ . Expressed in integral form

$$C(t) = \int_0^t P(t') dt' = \frac{\alpha}{\lambda} \int_0^t w(t') dt' \quad (7)$$

Thus, this growth model is a statement that the rate of return (or feedback efficiency) $\eta = \alpha\varepsilon$ on economic value C is a consequence of doing thermodynamic work w with efficiency ε to grow the interface between civilization and environmental resources. By growing the interface, civilization is able to draw more energy a , and do more work w , thereby closing the loop.

Now, returning to frameworks for CO₂ emissions forecasts, the SRES definition for energy productivity $f = P/a$ can be understood in light of the above. If Eq. 2 is combined with Eqs. 5 and 6, this yields the basic relations

$$\eta = P/C = \alpha\varepsilon = \lambda f \quad (8)$$

Therefore, energy productivity $f = P/a$ is related to the heat engine thermodynamic efficiency $\varepsilon = w/a$ and a fiscal expression for the feedback efficiency $\eta = P/C$ through the fixed, intrinsic quantities α and λ .

A schematic illustrating the economic growth model is shown in Fig. 2. A discussion of how it relates to more orthodox economic approaches is contained in Appendix B, where it is shown how such traditional economic concepts as inflation, savings and capital depreciation can be interpreted within a thermodynamic context. A straightforward consequence of Eqs. 5 and 6 is that the rate of growth of the global economy obeys the simple relation

$$\frac{d \ln P}{dt} = \eta + \frac{d \ln \eta}{dt} \quad (9)$$

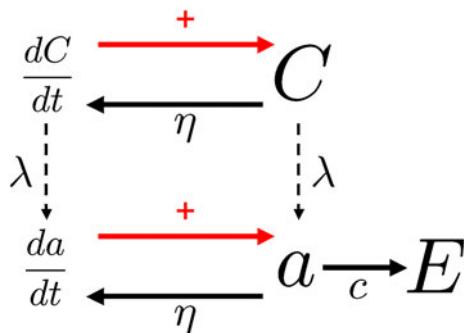


Fig. 2 Schematic extending Fig. 1 to relate the rate of energy consumption a by the human system to economic value C and CO₂ emissions E . Black arrows point in the direction of the product, red arrows in the direction of the integral over time. Work is done at rate w to enable energy consumption a to grow at rate $da/dt = \eta a$, where η is the feedback efficiency of a heat engine representing the system. The economy has a fixed relationship to energy consumption through $a = \lambda C$, where C is civilization's historical accumulation of real (inflation-adjusted) economic production of economic value $P = dC/dt$ (units currency), and λ is an intrinsic constant of proportionality. Thus, CO₂ emissions are related to economic production through $E = \lambda c \int_0^t P(t') dt'$, where c is the carbon content of energy in the fuel supply

Interestingly, the approach is of identical mathematical form to one often used to successfully model growth of vegetation, where vegetative “value” C refers not to money but instead to biomass, and P to the net primary productivity (Thornley and Johnson 1990; Montieth 2000). Presumably, biological organisms must also maintain a high potential interface with respect to their environment, enabling them to consume energy, produce heat and waste, and do work to incorporate the matter that enables them to grow (Vermeij 1995). Thermodynamic laws are fully general.

A difference between plants and civilization is that plant waste includes CO₂ that is recyclable, whereas the global economy creates most CO₂ from fossil-carbon, much of which accumulates in the atmosphere. From Fig. 2, CO₂ emissions can be represented simply through

$$E(t) = \lambda c C = \lambda c \int_0^t P(t') dt' \quad (10)$$

Present-day emissions are determined by past accumulation of real economic production and the current carbonization of the energy supply. Current emissions growth rates are given by

$$\frac{d \ln E}{dt} = \eta + \frac{d \ln c}{dt} \quad (11)$$

Equation 11 is more simple and physical than the expression for drivers in SRES forecasts given by Eq. 1.

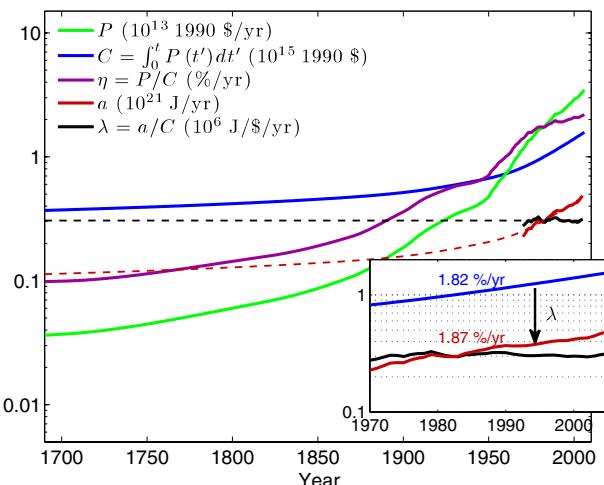
4 Evaluation

The preceding discussion argues for a direct theoretical link between anthropogenic emissions and basic thermodynamics. But is the argument observationally supported? The expression for emissions growth, Eq. 11, rests on the premise that there exists an intrinsic quantity λ representing how the historical accumulation of economic production C is supported by a rate of energy consumption a (Eq. 4). If λ is not constant with time, then the thermodynamic framework is false.

I examine this proposition now using statistics for the combination of world energy production a (Annual Energy Review 2006) and real global economic production P (United Nations 2007) (expressed here in fixed 1990 US dollars) for the 36 year interval between 1970 to 2005 for which these statistics are currently available. The time series for accumulated global economic value $C = \int_0^t P(t') dt'$ is estimated using sporadic calculations of P that have been ascertained for select years over the past two millennia (Maddison 2003) in combination with more recent annual records (United Nations 2007) to create a two-millennia yearly time-series in P (see Appendix C). Estimates of P and C and their ratio $\eta = P/C$ are shown in Fig. 3.

Figure 3 shows that, over a period between 1970 and 2005, the ratio $\lambda(t) = a/C$ maintained a nearly constant value of 0.306 exajoules per trillion 1990 US dollars per year, or alternatively 9.7 mW per 1990 dollar. Corrected for autocorrelation in the time-series, the observational uncertainty at the 95% confidence level is just ± 0.3 mW per 1990 dollar. The simplest interpretation is that this result supports the cornerstone hypothesis given by Eq. 4: the historical accumulation of real economic value through real economic production is maintained by continuous primary energy

Fig. 3 Estimates of gross world product P in market exchange rate, 1990 US dollars and economic value C , defined by $P = dC/dt$. Also shown are recent global primary energy consumption a , the ratio $\lambda = a/C$, and the feedback efficiency $\eta = P/C$. Dashed lines correspond to extrapolations based on assuming $\lambda = 9.7$ mW per 1990 US dollar



consumption; the relationship between value and rates of energy consumption is a constant parameter.

Of course it is possible that this observed result only holds over the 36-year period for which global energy consumption statistics are available, but it is expected theoretically; the period examined covers over half of total historical growth in a and C , and two thirds of P ; and, the observational uncertainty is small enough to plausibly reflect errors or noise in historical data. For example, new primary energy production (what has been measured) only reflects new primary energy consumption (what is theoretically relevant) in the average, not the instant.

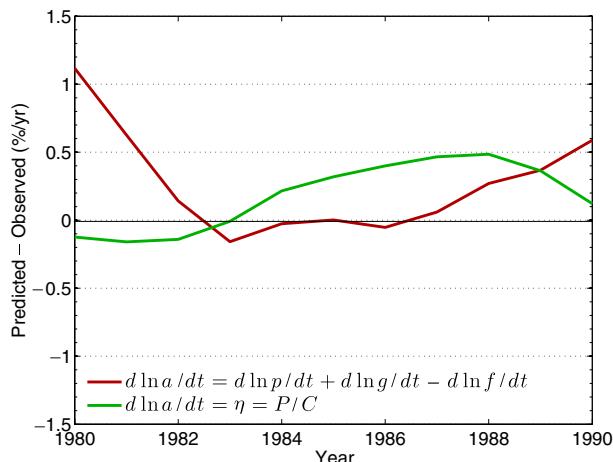
5 Drivers of emissions growth

The existence of a fixed relationship between energy production and accumulated real economic production simplifies the number of drivers required for CO₂ emissions forecasts. To see how, the SRES emissions growth equation (Eq. 1) can be equated with the more thermodynamic expression given by Eq. 11. Since both expressions rely on exogenous expressions for carbonization growth $d \ln c/dt$, this is effectively a comparison of expressions for growth in energy consumption $d \ln a/dt$

$$\frac{d \ln p}{dt} + \frac{d \ln g}{dt} - \frac{d \ln f}{dt} = \eta \equiv \lambda f \quad (12)$$

SRES models consider population p and standard of living g and energy productivity f as the key “drivers” of energy consumption growth, but the “driver” concept can be misleading when, at a very basic level, feedback determines how p , g , and f are inter-related. Equation 12 demonstrates that growth in p and g is fundamentally constrained by the sum of the current state of the feedback efficiency $\eta \equiv \lambda f$ and its rate of change $d \ln f/dt$. Therefore, knowledge of the behavior of only one parameter, f , is required for forecasts of energy consumption growth, rather than each of f , p and g .

Fig. 4 Difference between predicted and actual growth rates in global energy consumption a , based on predictions derived using persistence in trends (red) and the zeroth-order model presented here (green). Trend persistence is calculated using the prior 10 years as a basis; the zeroth-order model is based only on current year calculations of the feedback efficiency η . Hind-casts are compared with actual observed rates for a period covering the following 15 years



So, perhaps surprisingly, changes in population and standard of living might best be considered as only a response to energy efficiency. As part of a heat engine, creating people and their lifestyles requires energy consumption. Doing so efficiently merely serves to bootstrap civilization into a more consumptive (and productive) state. Likely, society has traditionally praised energy efficiency gains for precisely this reason. As summarized by Eq. 2, energy efficiency gains accelerate rather than slow energy consumption (Jevons 1865; Sorrell 2007), contrary to what is commonly assumed (Pacala and Socolow 2004).

This does not mean that consideration of population and standard of living in SRES models is invalid, of course, only that their evolution must be consistent with thermodynamic constraints (Eq. 12). Figure 4 shows a time-series comparing 15-year hind-casts with observations, evaluated for both sides of Eq. 12, in each of the years 1980 to 1990. Hind-casts based on growth of p , g and f apply straight-forward persistence in trends from the prior 10 years, i.e., $d \ln a / dt = d \ln p / dt + d \ln g / dt - d \ln f / dt$. For comparison, hind-casts based on the zeroth-order thermodynamic expression for economic growth need only employ evaluations of the current-year state of $\eta = P/C$.

Since both approaches reflect already realized thermodynamic constraints, both “persistence” and a thermodynamic model give hind-casts that reproduce observed trends with comparable accuracy. Notably, the thermodynamic model provides a hind-cast for average growth between 1990 and 2005 that is within just 0.1%/year of observed growth rates. A prior study found that this level of accuracy was only attained by a particular “worst-case” SRES model for this particular time period (Raupach et al. 2007). What is important here is that, for the purpose of future forecasts, the thermodynamic approach is accurate while being both simpler and more physical than using persistence or sophisticated SRES models.

6 Considerations for modeling future emissions scenarios

An advantage of appealing to energy efficiency in forecasts of CO₂ emissions is that $\eta = \lambda f$ tends to vary rather slowly. Since 1970, growth of $\eta = P/C$ has climbed from

1.4% per year to 2.1% per year in 2005 (Fig. 3), corresponding to an e-folding time-scale $\tau_\eta = 1/(d \ln \eta / dt)$ of approximately 100 years. Expressed in terms of time-series analysis, η is highly “reddened”, because it is an integrator of $d\eta/dt$. Alternatively, and in more fiscal terms, global economic value C (and hence energy consumption $a = \lambda C$) varies slowly because it is an integrator of economic production $P = dC/dt$ (Fig. 3). The present and future are influenced by even the most distant past, and the past cannot be erased.

The carbonization of the energy supply c , is changing even more slowly (see Appendix D) with a time scale of about 300 years. What this means is that future emissions rates for CO₂ are most strongly influenced by the current state of η . As a zeroth-order assumption, it is reasonable to assume persistence in η , meaning that over time-scales much less than τ_η , future emissions are unlikely to depart substantially from the recent growth rate of 2.1% per year.

More accurate forecasts of energy consumption and CO₂ emissions rates will require an understanding of how η itself evolves. Assuming c is a constant, positive values of $d \ln \eta / dt$ imply super-exponential growth² of CO₂ emissions E (c.f. Pielke et al. 2008). The solution for Eq. 11, starting at some time t_i , is

$$E = E_i \exp [\eta_i \tau_\eta (e^{\Delta t / \tau_\eta} - 1)] \quad (13)$$

Note, that growth condenses to the single exponential form in the limit of $\Delta t \ll \tau_\eta$.

However, in the long-term, even assuming persistence in $d \ln \eta / dt$ is an oversimplification since τ_η itself evolves. History shows bursts in efficiency growth, notably around 1880 and 1950, perhaps when important new discoveries of energy reservoirs made the past less relevant (Fig. 3). But, in both cases, the initial burst in η eventually tapered. After 1950, the time-scale τ_η , changed from just 30 years between 1950 and 1970, to 67 years between 1970 and 1990, and 120 years between 1990 and 2005. Plausibly, $1/\tau_\eta = d \ln \eta / dt$ will eventually cross zero and turn negative, implying sub-exponential growth in emissions E (Eq. 13).

Unfortunately, if $-d \ln \eta / dt$ is ever greater than η over the long term, while emissions growth may be significantly slowed, what is implied is a real global economy that is shrinking (Eq. 9). Robust multi-decadal forecasts of emissions E , and its relationship to economic production P , require a first principles thermodynamic model for how η changes with time. Assuming 1880 and 1950 were indeed associated with discovery of new energy reservoirs, this would suggest the problem is fundamentally geological, and that higher-order moments of η reflect rates of reservoir discovery and depletion.

Understood thermodynamically, the transfer of energy at rate a across the interface between energy reservoirs and civilization reflects a balance. On one hand, the transfer grows civilization, and increases the physical size of the interface ΔG . At the same time, however, it depletes the reservoirs, and this decreases ΔG . The sign and magnitude of the rate of work $w = d\Delta G / dt$, and therefore η , depends on the relative strengths of these two forces.

²Similar super-exponential growth behavior has been observed previously at a more local level, in the characteristics of cities (Bettencourt et al. 2007).

7 Mitigation

The premise behind mitigation is that there are “drivers” of emissions rates that can be meaningfully controlled through policy. As shown above, it is not clear that the driver concept is in fact meaningful. Rather, it appears that drivers in the Kaya Identity are merely a thermodynamic response to the current value of η .

At least this appears to be true for population p and standard of living g . It is not yet clear whether it applies to the current carbonization of the economy c . An interesting result that can be derived from Eq. 10 using the values for λ in Fig. 3 and c in Fig. 5 (Appendix D) is that the “carbon footprint” of civilization in recent decades reflects a simple relationship between the rate of global carbon emissions E and the accumulation over history of real global value C . The coefficient is $\lambda c = 5.2 \pm 0.2$ MtC per year, per trillion 1990 US dollars of global economic value.

To take the result further, Eq. 11 points towards a non-dimensional number

$$S = \frac{-d \ln c / dt}{\eta} \quad (14)$$

representing the relationship between the global economy’s rate of de-carbonization, $-d \ln c / dt$, and its rate of return, $\eta = \lambda f$. If $S \geq 1$, $d \ln E / dt \leq 0$, and emissions are stabilized or declining.

To reach stabilization, what is required is decarbonization that is at least as fast as the economy’s rate of return. Taking the 2005 value for η of 2.1% per year, stabilization of emissions would require an equivalent or greater rate of decarbonization. 2.1% of current annual energy production corresponds to an annual addition of approximately 300 GW of new non-carbon emitting power capacity—approximately one new nuclear power plant per day.

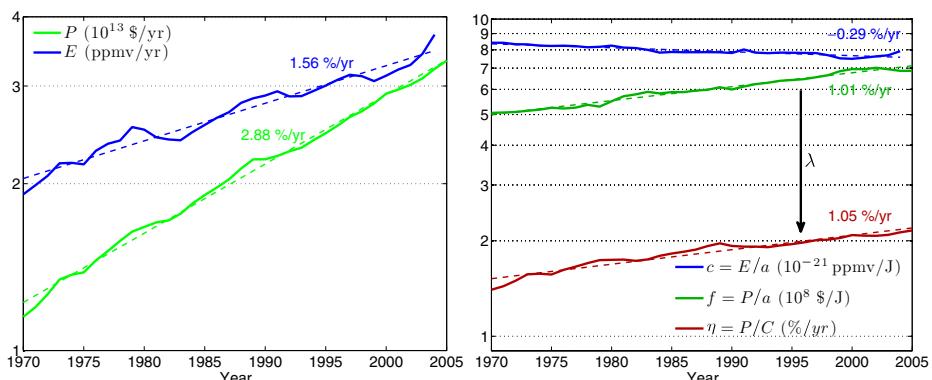


Fig. 5 For the period 1970 to 2005, trajectories in real global world production P and carbon dioxide emissions E (left), and feedback efficiency $\eta = P/C$ and the carbon dioxide emission intensity of energy $c = E/a$ (right). Here, c represents the increase in atmospheric concentrations of CO₂ E , per unit primary energy consumption a , that would be expected in a well-mixed atmosphere in the absence of terrestrial sink and source terms (1 ppmv CO₂ = 2.13 Gt emitted carbon (Trenberth 1981)). Dashed lines represent a least-squares first-order fit. Theoretical relationships between parameters are summarized in Table 1

Table 1 Mean observed and modeled rates for the period 1970 to 2005

Parameter	Model dependence	Observed mean (%/year)	Model mean (%/year)
Energy efficiency growth	$d \ln \eta / dt$	1.05	–
Carbonization growth	$d \ln c / dt$	−0.29	–
Feedback efficiency	$\eta = \eta_i \exp\left(\frac{d \ln \eta}{dt} t\right)$	1.84	–
Energy productivity growth	$d \ln f / dt$	1.01	1.05
Energy consumption growth	$d \ln a / dt = \eta$	1.87	1.84
Economic value growth	$d \ln C / dt = \eta$	1.82	1.84
Economic production growth	$d \ln P / dt = \eta + d \ln \eta / dt$	2.88	2.89
CO ₂ emissions growth	$d \ln E / dt = \eta + d \ln c / dt$	1.56	1.55

8 Conclusions

The physics incorporated into GCM representations of the land, oceans and atmosphere is required to adhere to universal thermodynamic laws. Ideally, the CO₂ emissions models meant for implementation in GCM projections of climate change should do so as well. Fortunately, it appears that appealing to thermodynamic principles may lead to a substantially constrained range of possible emissions scenarios. If civilization is considered at a global level, it turns out there is no explicit need to consider people or their lifestyles in order to forecast future energy consumption. At civilization's core there is a single constant factor, $\lambda = 9.7 \pm 0.3$ mW per inflation-adjusted 1990 dollar, that ties the global economy to simple physical principles. Viewed from this perspective, civilization evolves in a spontaneous feedback loop maintained only by energy consumption and incorporation of environmental matter.

Because the current state of the system, by nature, is tied to its unchangeable past, it looks unlikely that there will be any substantial near-term departure from recently observed acceleration in CO₂ emission rates. For predictions over the longer term, however, what is required is thermodynamically based models for how rates of carbonization and energy efficiency evolve. To this end, these rates are almost certainly constrained by the size and availability of environmental resource reservoirs. Previously, such factors have been shown to be primary constraints in the evolution of species (Vermeij 1995, 2004). Extending these principles to civilization, emissions models might be simplified further yet.

Acknowledgements This work was enabled by financial support from the NOAA Office of Global Programs and a NASA New Investigator Program award. The author is grateful for helpful feedback from Steven Sherwood, Geerat Vermeij, Claudio Holzner, Axel Kleidon, Clinton Schmidt, and Christopher Garrett.

Open Access This article is distributed under the terms of the Creative Commons Attribution Noncommercial License which permits any noncommercial use, distribution, and reproduction in any medium, provided the original author(s) and source are credited.

Appendix

A material transfer

To understand the details of the heat engine described in this article in a bit more detail, it is helpful to look more explicitly at what constitutes available energy and work for this case. The Gibbs energy potential of matter can be expressed as $\sum_i n_i \mu_i(T, p)$, where n_i refers to the number of the species i with specific chemical potential $\mu_i(T, p)$ (Zemansky and Dittman 1997; Job and Hermann 2006) (the “chemical” potential, rather confusingly, can always be generalized where relevant to incorporate the potential exothermic energy in nuclear bonds). The interface separating the entity and its environment may be composed of matter in many forms. However, a simplifying argument can be made that the potential difference ΔG can be split up into \check{n} arbitrary units of matter, each unit carrying an identical available potential of $\Delta\mu(T_s, p)$

$$\Delta G = \check{n} \Delta\mu(T_s, p) \quad (15)$$

Likewise, the net flux of material between the environment and the entity at rate dn/dt requires energy consumption by the system as a whole at rate

$$a = \frac{dn}{dt} \Delta\mu(T_s, p) \quad (16)$$

But, since $a = \alpha \Delta G$, it also holds that

$$a = \alpha \check{n} \Delta\mu(T_s, p) \quad (17)$$

Combined, Eqs. 16 and 17, imply that the intensive quantity $\alpha = 1/\check{n}(dn/dt)$ is determined by the particular physics relating the amount of high potential matter along the interface to the flux of matter across it.³

The evolution of energy consumption by the system, da/dt , is related to its rate of doing work through αw (Eq. 2), but more specifically to the interface’s material growth. Since work is defined by $w = d(\Delta G)/dt$, and the interface temperature and pressure are fixed, it follows that the potential defining the interface between the entity and its environment evolves at rate

$$w = \frac{d\check{n}}{dt} \Delta\mu(T_s, p) \quad (18)$$

Work is positive if the material interface grows. Expressed in terms of the rate of energy consumption,

$$w = \frac{d\check{n}}{dn} a = \frac{1}{\alpha} \frac{d \ln \check{n}}{dt} a = \frac{1}{\alpha} \frac{da}{dt} \quad (19)$$

³It is straightforward to show that for the special case of Maxwellian diffusion along a concentration gradient to, for example, a cloud droplet or snow flake (Pruppacher and Klett 1997), evolution of a and \check{n} is determined not by the surface area of the interface (as might initially seem more intuitive) but rather by a length dimension. In this case, α is determined by the product of the diffusivity of vapor in air and the area density of vapor at saturation.

Because the heat engine efficiency is given by $\varepsilon = w/a$, this leads to the result that

$$\varepsilon = d\check{n}/dn = \frac{1}{\alpha} \frac{d \ln \check{n}}{dt} \quad (20)$$

As a feedback loop, Eqs. 2 and 20 can be combined to show that the feedback efficiency η is

$$\eta = \frac{d \ln \check{n}}{dt} \quad (21)$$

Thus, η expresses the logarithmic growth of the number of elements defining the interface between the entity and its environment. If the net flow is from the environment to the entity, the portion of material that diffuses across the interface and does not contribute to interface growth is returned to the environment as waste.

B Comparison with traditional economic models

Economic studies normally separate production into two components: a fraction s representing a savings, or investment; and a fraction $(1 - s)$ representing private and government “consumption”. Models represent the nominal growth in “capital” K (units currency) as the difference between the portion s of production P (units currency per time) that is a savings or investment, and capital depreciation at rate γ

$$\frac{dK}{dt} = (P - W) - \gamma K = sP - \gamma K \quad (22)$$

where individual and government consumption is represented by $W = (1 - s) P$.

In return, according to some functional form, labor L (units worker hours) employs capital K (units currency) to generate further production P (units currency per time). For the sake of illustration, a commonly used representation is the Cobb-Douglas production function

$$P = AK^\alpha L^{1-\alpha} \quad (23)$$

where A , the “total factor productivity”, is a compensating factor designed to account for any residual unaccounted for by K and L . The exponent α is empirically determined. The Solow Growth Model (Solow 1957) expresses the prognostic form for Eq. 23 as

$$\frac{d \ln P}{dt} = \frac{d \ln A}{dt} + \alpha \frac{d \ln K}{dt} + (1 - \alpha) \frac{d \ln L}{dt} \quad (24)$$

Commonly, the term $d \ln A/dt$ is interpreted to represent technological progress.

There have been criticisms raised of the Solow Model because it makes no explicit reference to natural resources (Georgescu-Roegen 1993; Ayres et al. 2003). One suggested remedy has been to incorporate primary energy consumption into Eq. 23 as a complement to labor or capital (Saunders 1992, 2000), in which case

$$P = (A_K K)^\alpha (A_L L)^\beta (A_a a)^{1-\alpha-\beta} \quad (25)$$

where, again, a is energy consumption, α and β are empirically determined, and the subscripts for A refer to respective technological progress.

Now, by comparison, in the thermodynamic economic growth model introduced here, real (inflation-adjusted) economic production P (units currency per time)

and global value C (units currency) are, respectively, fiscal representations of net thermodynamic work and the rate of consumption of available primary energy resources. The economic growth model described by Eqs. 5 and 6 is given by the value production function

$$P = \eta C \quad (26)$$

where η is the feedback efficiency representing a rate of return due to thermodynamic work by the system on the system. The equation for growth of value is

$$dC/dt = P \quad (27)$$

Note that while C is analogous to capital K in Eq. 22, since $C = a/\lambda$, it is a more explicitly thermodynamic expression of value.

So, to put the above in context of standard economic production functions, Eq. 26 can be considered to be a simplification of Eq. 25. The representation of economic value C employed here is a substitution of the combination of traditionally defined capital K and labor L in Eq. 25, such that $\alpha = 1$ and $\beta = 0$, and $A_K = \eta$. Alternatively, since C is itself only a monetary representation of the rate of primary energy consumption a through $a = \lambda C$, it could equally be stated that $\alpha = \beta = 0$, and $A_a = \eta/\lambda$.

Note that the thermodynamic production function (Eq. 26), unlike more standard formulations (Eq. 23), has the mathematical advantage of being dimensionally self-consistent, as it does not need to appeal to non-integer exponents α and β of dimensional terms (such as L and K), as fitted to a specific set of circumstances, and with no certain application to different economic regimes.

It might be argued, however, that the model introduced here fails by leaving no room for either consumption W or depreciation γK , two central components of the standard economic growth equation (Eq. 22). Offhand, this seems reasonable because, certainly, some portion of economic production must be consumed, at least in order to maintain economic capital against depreciation or decay: buildings crumble; bodies must be maintained; old technology becomes obsolete; as does past acquisition of human skills and knowledge.

But these concerns can be resolved once it is recognized that the equations derived for this study are intended to apply only to real, inflation-adjusted production P , and not nominal production \hat{P} . To demonstrate, assume inflation is positive, in which case nominal value \hat{C} grows faster than real value by some fractional rate of real value, γ

$$\frac{d\hat{C}}{dt} = \frac{dC}{dt} + \gamma C \quad (28)$$

Since it has been argued here that $dC/dt = P$, this leads to

$$\frac{dC}{dt} = \hat{P} - \gamma C \quad (29)$$

in which case, the source of real value is nominal production, and the corresponding sink for real value occurs at rate γ . So, in fact, Eq. 29 illustrates that Eq. 27 does account for depreciation through the term γC , and is thus similar to the depreciation term γK in the standard growth equation for capital (Eq. 22). While depreciation is implicit when the growth equations are expressed in real, inflation-adjusted terms, depreciation is explicit when they are expressed in nominal terms.

In fact, it is interesting to see what the value decay rate γ represents. Again, because $dC/dt = P$, this means Eq. 27 leads to the statement $\hat{P} - P = \gamma C$. Alternatively, when nominal production is expressed in energy consumption co-ordinates through substitution of the expression $a = \lambda C$

$$\hat{P} - P = \gamma C = \frac{\gamma}{\lambda} a \quad (30)$$

Compare this to an equivalent expression derived for real production $P = (\eta/\lambda)a$ (Eq. 5). The implication here is that economic inflation, the difference between nominal and real production, is a consequence of the spontaneous decay or depreciation of total economic value C at rate γC . Put another way, since $P = \eta C$, the ratio $\gamma/(\gamma + \eta)$ is the fraction of nominal production \hat{P} that, unlike P , does not return itself as a real addition to total value C . In thermodynamic terms, value depreciation γC is an energy barrier that must first be crossed for real production to occur. If it is not, the perspective of civilization is that nominal production may be positive, but real production is negative. Net work w is done on civilization by the environment, rather than the reverse. Whenever this occurs, the interface between civilization and its environment ΔG decays.

There is also a consumption term in the traditional expression for capital growth (Eq. 22) that is not present in the thermodynamic expression for total value growth (Eq. 27). As it is normally defined, consumption is the portion of economic production that does not represent an investment or savings in traditional representations of capital K . By contrast, in the thermodynamic model, effectively all real production is an “investment” in total economic value C . While a portion of nominal production or nominal work may merely serve to offset depreciation of C as described above, all of the remainder adds to the total. Real production is net production.

To illustrate, the construction of coal mines and power plants clearly represents an investment in economic value in either framework. A less obvious, although functionally equivalent example, is food consumption. In standard representations, food would be “consumed” by households and not contribute to their value. However, the available chemical potential in food consumption $dn/dt\Delta\mu$ (Eq. 16) also maintains and improves that household’s capacity to further consume energy and do work by supporting its internal potential energy ΔG (Eq. 1). Of course, the consumption of an ordinary sandwich may only offset a body and mind against decay from “heat” loss, maintaining its internal potential such that it can continue to consume energy at the same rate it has in the past (in which case the real production rate P and net work rate w is zero since $\hat{P} = \gamma C$). The added value of a really good, if more expensive, sandwich is its capacity to facilitate real production and new energy consumption above and beyond decay (in which case real production is greater than zero and $\hat{P} > \gamma C$). The addition to total global value C (and internal potential ΔG) may derive from a heightened sense of personal well-being and an increased desire to productively interact with the rest of civilization in order to afford such sandwiches.

It is worth noting that a primary conclusion of this paper, that feedback loops in the economic system mean that increases in energy efficiency correspond to greater energy consumption, has been reached previously by some economists, albeit in a less explicitly physical form than presented here (Ayres et al. 2003; Saunders 1992, 2000; Khaazzoom 1980; Brookes 1990; Alcott 2005; Polimeni and Iorgulescu Polimeni 2006; Dimitropoulos 2007; Herring and Roy 2007). Although the concept was first

introduced by W. Stanley Jevons over a century ago (Jevons 1865), the extent of energy efficiency “rebound” or “backfire” remains disputed (Sorrell 2007), with no consensus among economists on how it should be quantified on the global scales relevant to forecasts of climate change from anthropogenic CO₂.

C Materials and methods for time series estimates

US Department of Energy statistics for global primary energy production (Annual Energy Review 2006) include fossil fuel, hydroelectric, nuclear, geothermal, wind, solar, and biomass sources. It is assumed here that production and consumption rates are, at least on average, equivalent. United Nations time series for world economic production (United Nations 2007) represent the total gross domestic product of all countries, adjusted for inflation and market exchange rates to fixed 1990 US dollars. Statistics for CO₂ emissions are obtained from the Carbon Dioxide Information Analysis Center (Marland et al. 2007). Rather than looking at nations or sectors, only global quantities are considered here because, at this level, atmospheric CO₂ is well-mixed, and international markets make details in economic trade unimportant.

Gross World Product estimates in 1990 market exchange rate dollars are available for each year since 1970 (United Nations 2007). Long-term but intermittent historical estimates are available for the years 1 to 1992 CE (Maddison 2003). The latter data set is expressed in Geary Khamis purchasing power parity (PPP) 1990 US dollars. In general, the motivation for expressing valuation in PPP instead of exchange rate dollars is to account for disparities in product valuation that exist between countries. In PPP dollars, product valuation is equalized according to its apparent contribution to standard of living. Countries with a low standard of living tend to have a relatively high gross domestic product when expressed in PPP rather than market exchange rate dollars because equivalent products and services tend to be less expensive.

However, because the focus of this study is energy production and associated CO₂ emissions, rather than national standard of living, it is historical records of market exchange rate valuations that are used. Exchange rate measures of production P are assumed to most accurately reflect the total energy costs associated with manifesting products and services in the respective nations where they are consumed.

To account for any discrepancy between PPP and exchange rate estimates in historical records for economic production P , market exchange rate data from 1970 onwards is used to devise a time-dependent correction factor π to be applied to PPP records such that $\pi = \text{PPP/exchange rate}$. For the period 1970 to 1992, during which both PPP and market exchange rate estimates of P are available, the fitted value for π is $\pi = 1 + 0.258 \exp[(t - 1998)/73]$. This correction factor can be extrapolated and applied to all PPP data between the years 0 and 1969. For the period from 1970 onwards, measured exchange rate values are used. Because the historical estimates of P in PPP dollars are increasingly sparse with distance back in time (e.g. there are only three data points for the period 1 to 1500 CE), the corrected dataset for P is mapped to a yearly distribution using a cubic spline fit.

Estimates of economic value C represent an accumulation of economic production P over time since 1 CE, i.e., $C(t) = C(1) + \int_1^t P(t') dt'$. To estimate a value for $C(1)$, it is assumed that the ratio of population to economic value in 1 CE. is equivalent to the average value between 1 CE and the threshold of the industrial revolution circa 1700 CE. From historical population statistics (Maddison 2003), the associated

iterative solution for $C(1)$ is 120 trillion 1990 U.S. dollars. For comparison, the estimated value of C in 2005 CE is 1580 trillion 1990 US dollars (Fig. 3). Although, off-hand, this value for $C(1)$ seems surprisingly high, it is still very small compared to current day values, so the derived value of λ presented in this paper is relatively insensitive to errors in its estimate.

D Summary of observed growth rates between 1970 and 2005

A summary of observed growth rates in global world real production P , carbon dioxide emission rates E , feedback efficiency η and carbon dioxide emission intensity c between 1970 and 2005 is provided in Fig. 5 and in Table 1, along with relevant equations based on the thermodynamic economic growth model described here.

References

- Alcott B (2005) Jevons' paradox. *Ecol Econ* 54:9–21. doi:[10.1016/j.ecolecon.2005.03.020](https://doi.org/10.1016/j.ecolecon.2005.03.020)
- Annual Energy Review (2006) Tech. Rep. DOE/EIA-0384(2006). Department of Energy, Energy Information Administration. www.eia.doe.gov/aer/inter.html
- Ayres RU, Ayres LW, Warr B (2003) Exergy, power and work in the US economy, 1900–1998. *Energy* 28:219–273. doi:[10.1016/S0360-5442\(02\)00089-0](https://doi.org/10.1016/S0360-5442(02)00089-0)
- Bettencourt LMA, Lobo J, Helbing D, Kühnert C, West GB (2007) Growth, innovation, scaling, and the pace of life in cities. *Proc Natl Acad Sci U S A* 104:7301–7306
- Brookes LG (1990) The greenhouse effect: the fallacies in the energy efficiency solution. *Energy Policy* 18:199–201
- de Groot SR, Mazur P (1984) Non-equilibrium thermodynamics. Courier Dover, New York
- Dimitropoulos J (2007) Energy productivity improvements and the rebound effect: an overview of the state of knowledge. *Energy Policy* 35:6354–6363
- Georgescu-Roegen N (1993) Valuing the Earth: economics, ecology, ethics, chap. The entropy law and the economic problem. MIT, Cambridge, pp 75–88
- Herring H, Roy R (2007) Technological innovation, energy efficiency design and the rebound effect. *Technovation* 27:194–203
- IPCC WG III (2007) Climate change 2007: mitigation of climate change. In: Metz B, Davidson OR, Bosch PR, Dave R, Meyer LA (eds) Contribution of working group III to the fourth assessment report of the intergovernmental panel on climate change. Cambridge University Press, Cambridge, United Kingdom and New York, NY, USA
- Jevons WS (1865) The coal question. Macmillan, New York
- Job G, Hermann F (2006) Chemical potential—A quantity in search of recognition. *Eur J Phys* 27:353–371. doi:[10.1088/0143-0807/27/2/018](https://doi.org/10.1088/0143-0807/27/2/018)
- Khazzoom JD (1980) Economic implications of mandated efficiency in standards for household appliances. *Energy J* 1:21–40
- Kleidon A (2004) Beyond Gaia: thermodynamics of life and earth system functioning. *Clim Change* 66:271–319
- Maddison A (2003) The world economy: historical statistics. OECD
- Marland G, Boden TA, Andres RJ (2007) Trends: a compendium of data on global change, chap. Global, regional, and national CO₂ emissions. Carbon Dioxide Information Analysis Center, Oak Ridge National Laboratory, U.S. Department of Energy, Oak Ridge
- Montieth JL (2000) Fundamental equations for growth in uniform stands of vegetation. *Agric For Meteorol* 104:5–11
- Nakicenovic N (2004) Socioeconomic driving forces of emissions scenarios. In: Field CB, Raupach MR (eds) The global carbon cycle. Island, Montague, pp 225–239
- Pacala S, Socolow R (2004) Stabilization wedges: solving the climate problem for the next 50 years with current technologies. *Science* 305:968–972. doi:[10.1126/science.1100103](https://doi.org/10.1126/science.1100103)
- Pielke R Jr, Wigley T, Green C (2008) Dangerous assumptions. *Nature* 452:531–532
- Polimeni JM, Iorgulescu Polimeni R (2006) Jevon's paradox and the myth of technological liberation. *Ecol Complex* 3:344–353. doi:[10.1016/j.ecocom.2007.02.008](https://doi.org/10.1016/j.ecocom.2007.02.008)

- Pruppacher HR, Klett JD (1997) Microphysics of clouds and precipitation, 2nd rev. edn. Kluwer Academic, Dordrecht
- Raupach MR, Marland G, Ciais P, Le Quéré C, Canadell JG, Klepper G, Field C (2007) Global and regional drivers of accelerating CO₂ emissions. Proc Natl Acad Sci U S A. doi:[10.1073/pnas.0700609104](https://doi.org/10.1073/pnas.0700609104)
- Saunders HD (1992) The Khazzoom-Brookes postulate and neoclassical growth. Energy J 13:131–148
- Saunders HD (2000) A view from the macro side: rebound, backfire, and Khazzoom-Brookes. Energy Policy 28:439–449
- Schrödinger E (1944) What is life? The physical aspect of the living cell. The University Press, Berkeley
- Solow RM (1957) Technical change and the aggregate production function. Rev Econ Stat 39:312–320
- Sorrell S (2007) The rebound effect. Tech. rep., UKERC
- Stott PA, Kettleborough JA (2002) Origins and estimates of uncertainty in predictions of twenty-first century temperature rise. Nature 416:723–725
- Thornley JT, Johnson IR (1990) Plant and crop modelling. Clarendon Press, Clarendon
- Trenberth KE (1981) Seasonal variations in global sea level pressure and the total mass of the atmosphere. J Geophys Res 86:5238–5246
- United Nations (2007) United Nations statistical databases. unstats.un.org/unsd/snaama
- Vermeij G (1995) Economics, volcanoes, and Phanerozoic revolutions. Paleobiology 21:125–152
- Vermeij GJ (2004) Nature: an economic history. Princeton University Press, Princeton
- Zemansky MW, Dittman RH (1997) Heat and thermodynamics, 7th edn. McGraw-Hill, New York